| Department of Energy and Sustainable Energy | Mathematics 3 | Mid-Term Exam-2 |
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| Answer All questions $\quad$ Duration: 1 Hour | December 2016 | 20 Marks |

[1] Show that $u(x, y)$ is harmonic where $u=e^{x} \sin y$.
[2] Show that $\mathrm{f}(\mathrm{z})$ satisfies Riemman's equations where $f(z)=z+\cos z$
[3] Find the residues of the function : $f(z)=\frac{z-1}{(z+3)(z-2)}$
[4] Show that: If $C$ is the circle $|z|=4$. Then
(a) $\int \frac{\cos z}{z} d z=2 \pi i$
(b) $\int \frac{\mathrm{c}}{\mathrm{c} \mathrm{z}^{2}-1} \mathrm{dz}=2 \pi \mathrm{i}$
(c) $\int \frac{\mathrm{z} \cdot \sin \mathrm{z}}{\mathrm{z}-6} \mathrm{dz}=0$

